Eleventh Slovenian Crystallographic Meeting Bohinj, Slovenia, 27 – 30 June 2002

# Phase Transitions in Modulated Structures

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## Contents

Introduction

Short review on structural phase transitions

Example: **Bi**<sub>2</sub>**Ti**<sub>4</sub>**O**<sub>11</sub>

Introduction to structural modulation

Phase transitions in modulated structures.

Example: Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>



New mechanisms in 2. order phase transitions.



# What is basic knowledge on structural phase transitions ?

## Introduction

#### **Structural Phase Transition:**

A sudden change of the structure symmetry on the variation of thermodynamic parameters.

<u>Classification</u> of structural phase transitions.

1. Order Phase Transition.

at  $T_c: \Delta S \neq 0$  $\Delta V \neq 0$ 

<u>Mechanism :</u> Nucleation and growth <u>Characteristic property</u>: Thermal hysteresis • 2. Order Phase Transition. at  $T_c$ :  $\Delta S = O$ 

 $\Delta V = 0$ 

<u>Mechanism :</u> Continuous Transition <u>Characteristic property</u>: Landau theory applies

#### Example: **Bi**<sub>2</sub>**Ti**<sub>4</sub>**O**<sub>11</sub>

Lattice parameter **b** 

Sequence of phases

Introduction



#### Superstructure reflection

215

195

Intensity



#### Spontaneous strain



### Example: **Bi<sub>2</sub>Ti<sub>4</sub>O**<sub>11</sub>

#### Structure : α-phase

Introduction



#### Structure : β-phase

**Bi - Atoms** 



#### Mechanism:

Continuous shift of Bi-atoms off the mirror plane Phase transition is triggered by the ordering of the lone pair of Bi.

# Structural modulation

# What is the basic knowledge on structural modulation ?

#### Structural modulation

Modulation: The atomic parameters of a structure are affected by periodic functions of long periods. The ratio between the periods of the HT-phase and the modulated phase is a small rational number Commensurate structure The ratio between the periods of the HT-phase and the modulated phase is not a small rational number

Incommensurate structure

Typical sequence of phases:



### Phase Transitions in modulated structures

### Example: Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

#### Sequence of phases:



Diffraction pattern at RT:



#### Example: Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>



Variation of the q-vector





Satellite intensity

#### Example: Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

The structure of the commensurate LT - phase:

Characteristic feature: Centers of 6-fold coordinated Calcium are ordered in octagons.



#### <u>Example</u>: $Ca_2CoSi_2O_7$

<u>Claim</u>: The modulated structures are different degrees of condensations of octagonal clusters with 6-fold coordinated Calcium:

# The structure of the commensurate LT - phase:



# The structure of the incommensurate phase:



#### Example: Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

<u>Proof</u>: TEM pictures of the IC-phase at RT ; octagonal rings with the size of the rings of 6-fold coordinated Calcium:



After Van Heurk et al., 1992



### What is new for 2. order phase transitions?

#### Superstructure reflection







$$(Ca_{1-x}Sr_{x})_{2}MgSi_{2}O_{7}; x = 0.16$$





$$Tc = 277 \text{ K} \quad ? \quad \Longleftrightarrow \quad ? \quad Tc = 250 \text{ K}$$

Transformation temperature

# TEM diffraction pattern of the incommensurate phase $(Ca_{1-x}Sr_x)_2MgSi_2O_7$ .



After M. Schosnig et al., 2000

## Example: **Bi<sub>2</sub>Ti<sub>4</sub>O**<sub>11</sub>

#### Structure : α-phase



#### Structure : β-phase

**Bi - Atoms** 



#### Mechanism:

Continuous shift of Bi-atoms off the mirror plane Phase transition is triggered by the ordering of the lone pair of Bi.

The new interpretation of a 2. order phase transition:

- A 2. order phase transition does not occur at a point, the Landau concept is valid far above and far below the transition .
- Fluctuations determine the temperature regime around a phase transition.
- Structural motives of the LT phase with short range order exist far above the transition as precursors in the HT phase. There is a continuous variation of the degree of order with temperature.
  - The definition of a "transition temperature" has some arbitrariness.



**Order parameter** 

### Example: NaNO<sub>2</sub>

#### Reciprocal space:

