# Mechanisms at Structural Phase Transitions

H. Böhm

Institut für Geowissenschaften Universität Mainz Germany

V. Kahlenberg, J. Kusz, O. Pawlig, M. Riester

### Definition

### **Structural Phase Transition:**

It occurs in a crystalline solid with a sudden change in symmetry because of a change of pressure and/or temperature.

A change of the symmetry is associated with the change of the structure.

### classification

First order phase transitions.

at the temperature  $T_c$ :  $\Delta S \neq 0$ 

 $\Delta V \neq 0$ 

#### Mechanisms:

nucleation and growth,

range of coexisting phases

characteristic features:

thermal hysteresis

#### classification

Second order phase transitions.

at the temperature 
$$T_c$$
:  $\Delta S = O$ 

$$\Delta V = 0$$

#### Mechanisms:

continuous transition

<u>characteristic feature</u>:

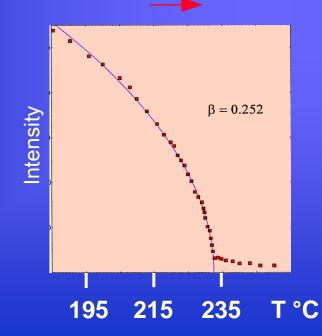
no thermal hysteresis;

Landau Theory is applied

### Sequence of phases

$$lpha$$
 - Phase C2/c

$$c_0(\alpha) = 2 c_0(\beta)$$
 $Tc = 233 °C$ 

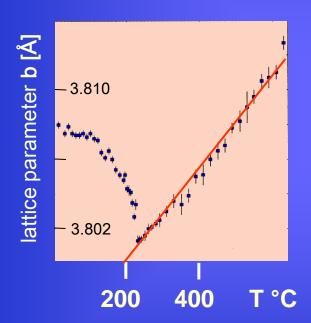


$$\sqrt{I} \sim \eta = \eta_0 (T_c - T)^{\beta}$$
 $\eta = \text{order parameter}$ 

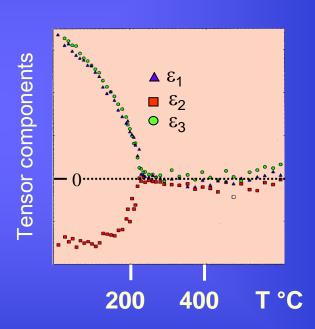
Superstructure reflection

Bi<sub>2</sub>Ti<sub>4</sub>O<sub>11</sub>





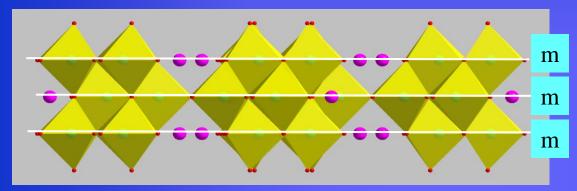
#### Spontaneous strain



No thermal hysteresis: 2.nd order phase transition , coupling between  $\eta$  and the spontaneous strain

# $\mathrm{Bi_{2}Ti_{4}O_{11}}$

structure : β-Phase

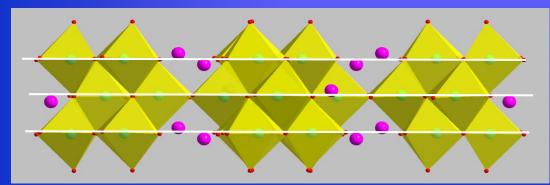


Interpretation in terms of the Landau Theory:

At Tc a continuous shift of the Bi-atoms begins off the mirror plane.

structure : α-Phase

**Bi - Atome** 



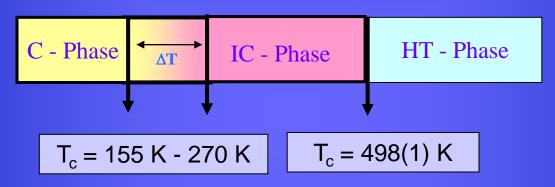
Comment:

The transition is triggered by the ordering of the lone electron pair of Bi.

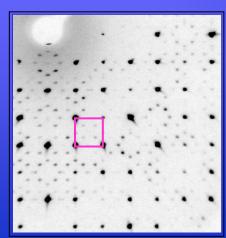
# Example

### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

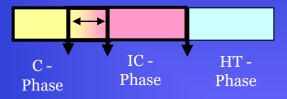
#### Sequence of phases:

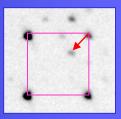


Diffraction pattern at RT:

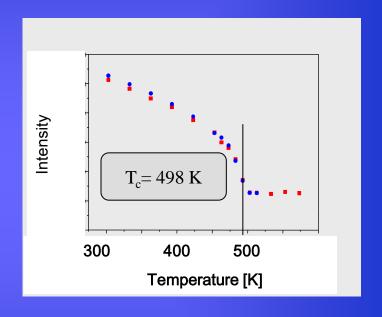


### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>





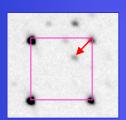
Satellite-Intensity



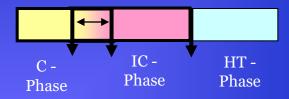
Phase transition at about 500 K

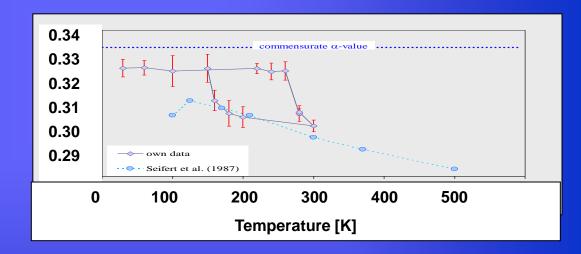
No thermal hysteresis: 2.nd order phase transition

### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>



Variation of the q-vector (incommensurate phase)



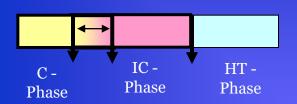


Phase transition between 155 K und 270 K

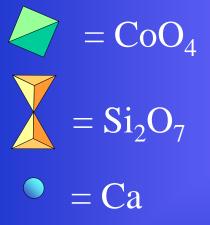
#### Thermal hysteresis:

1. order phase transition

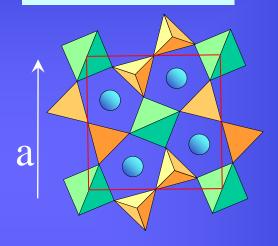
#### continued Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

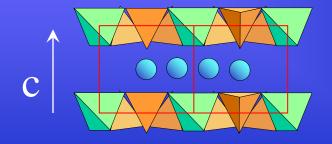






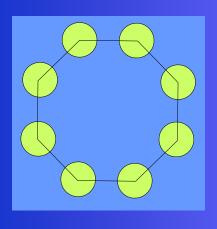
### HT - Phase



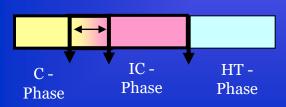


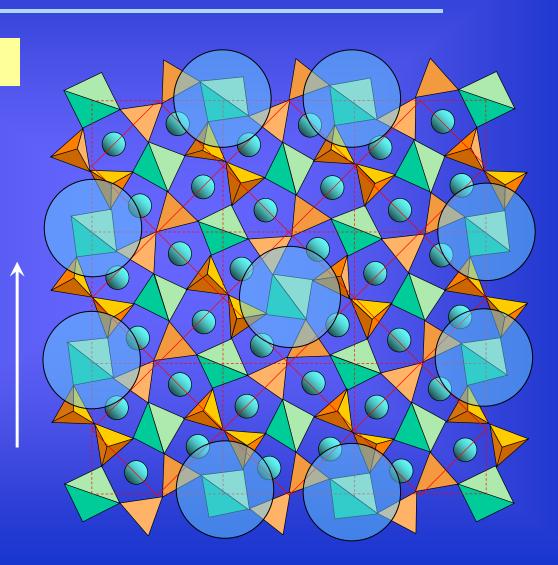
### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

### C - Phase

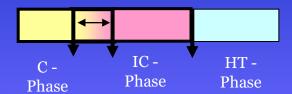


3.a



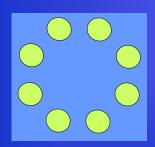


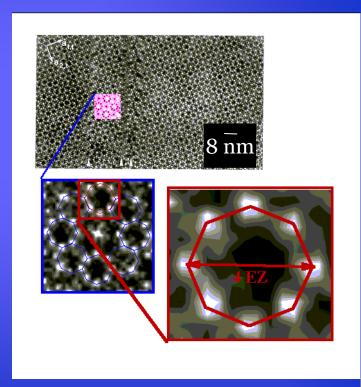
### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>



IC - Phase

HRTEM picture at RT: Octagonal rings.

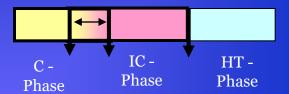


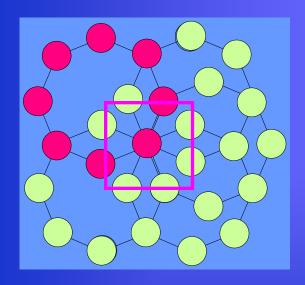


Van Heurk et al., 1992

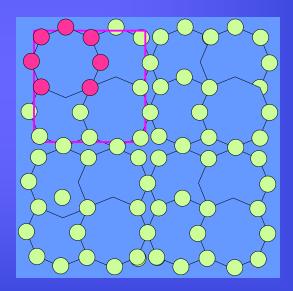
### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

Relationship between the phases





C-Phase: An ordered superposition of octagonal rings.

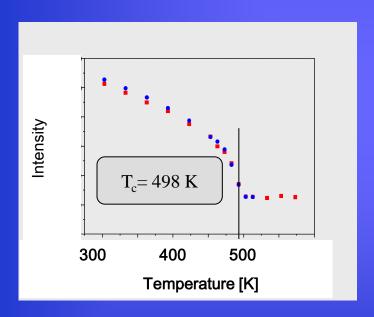


IC-Phase: An arbitrary superposition of octagonal rings.



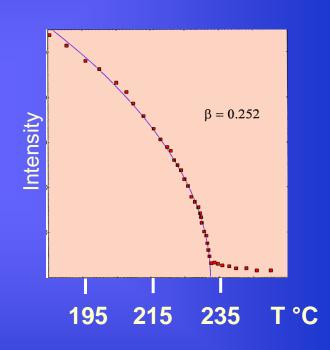
# Mechanisms

Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>



Satellite reflection

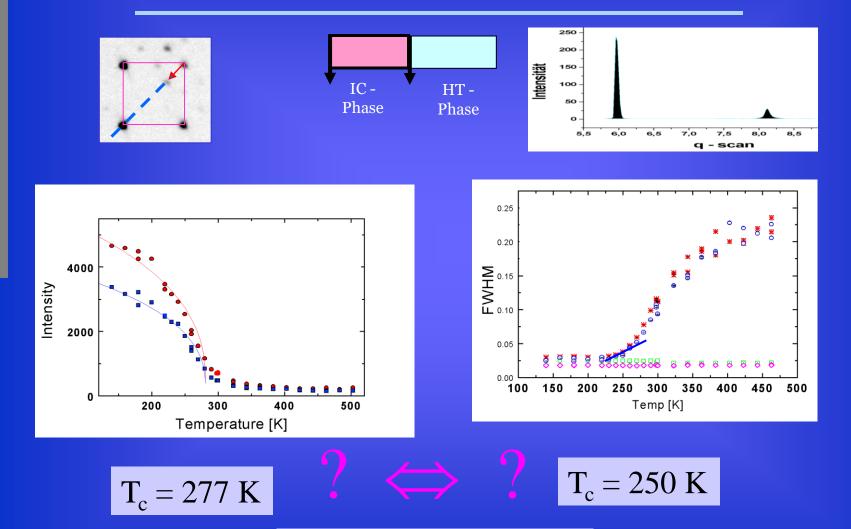
Bi<sub>2</sub>Ti<sub>4</sub>O<sub>11</sub>



Superstructure reflection

### Mechanisms

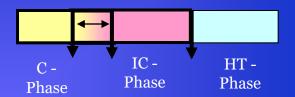
### $(Ca_{1-x}Sr_x)_2MgSi_2O_7; x = 0.16$

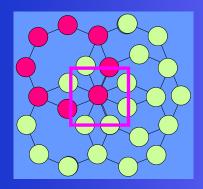


Transformation temperature

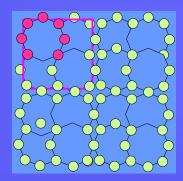
### Ca<sub>2</sub>CoSi<sub>2</sub>O<sub>7</sub>

### Relationship between the phases

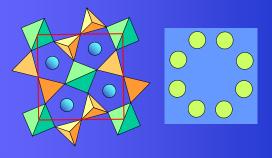




C-Phase: An ordered superposition of octagonal rings.



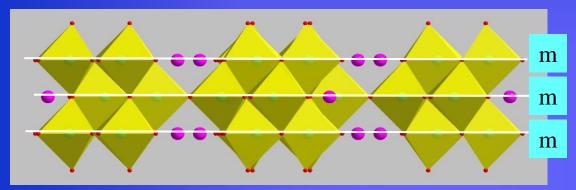
IC-Phase: An arbitrary superposition of octagonal rings.



HT-Phase:
Domains of octagonal rings with short range order.

# Bi<sub>2</sub>Ti<sub>4</sub>O<sub>11</sub>

structure : β-Phase

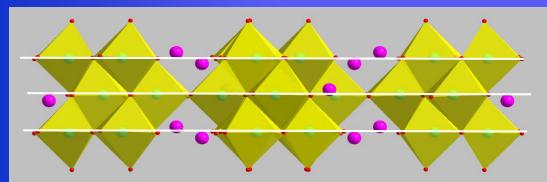


#### <u>Interpretation:</u>

Above T<sub>c</sub> the lone pair of Bi-atoms begins to order in domains with short range order.

structure :  $\alpha$ -Phase

Bi - Atome



Long range order is attained at the transition point

# Final question

What characterizes a continuous phase transition?

#### Answer:

The continuous increase of the range of order until long range order is achieved (not a continuous shift of atomic positions).