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# 1 History of Glass

Encyclopedia, 10.1 - 10.10

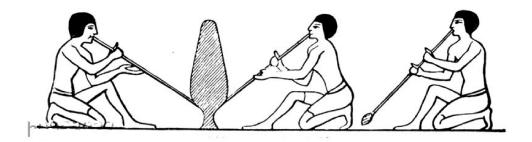




Figure 4 (a) Egypt (cosmetic jug, 18th dynasty, 24 × 30 cm; British Museum 22819); (b) Ur, Mesopotamia (flutted glass bottle, height 11.8 cm; BM 120659). Source: (a, b): ◎ The Trustees of the British Museum.

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Marco Verità

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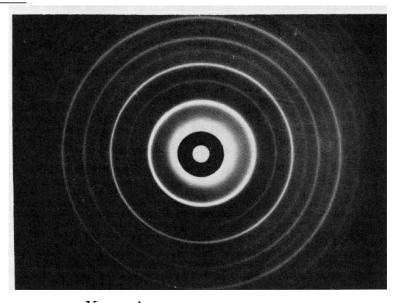
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Marie-Hélène Chopinet and Pascal Richet

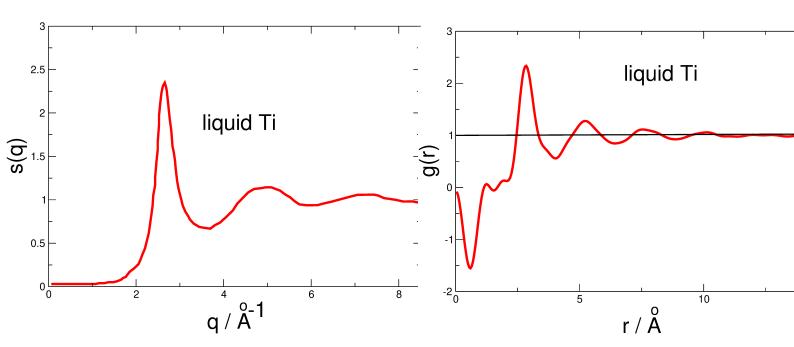
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## 2 Hard-Sphere Percus-Yevick Theory for S(q) and g(r)

## Schirmacher, 2.8



X-ray image



S(q) = Intensity from the middle outwards g(r)

S(q) = X-Ray- and neutron-scattering structure factor [1, 2]

$$S(q) = 1 + \rho_0 \int_{-\infty}^{\infty} d^3 \mathbf{r} e^{i\mathbf{q}\mathbf{r}} \left[ \mathbf{g}(\mathbf{r}) - 1 \right]$$
$$= 1 + 4\pi \rho_0 \int_0^{\infty} dr r^2 \frac{\sin(qr)}{qr} \left[ \mathbf{g}(\mathbf{r}) - 1 \right]$$

Here  $\rho_0 = N/V$  is the number density of the particles.

The radial distribution function g(r) gives the statistics of distances r between the molecules

Direct Correlation function c(r) (Ornstein, Zernike [2])

$$h(r) = g(r) - 1 = c(r) + \rho_0 \int d^3 \mathbf{r}' c(|\mathbf{r} - \mathbf{r}'|) c(r') + \dots + \dots$$
(1)
$$= c(r) + \rho_0 \int d^3 \mathbf{r}' h(|\mathbf{r} - \mathbf{r}'|) c(r')$$
(2)
$$= c(r) + \rho_0 [h \circ c](r)$$

$$\Rightarrow \rho_0 h(q) = \left[ S(q) - 1 \right] = \rho_0 c(q) \left[ 1 + \rho_0 h(q) \right]$$

$$\Rightarrow \rho_0 h(q) = \frac{\rho_0 c(q)}{1 - \rho_0 c(q)} = \underbrace{\frac{1}{1 - \rho_0 c(q)}}_{S(q)} - 1$$

$$\Rightarrow S(q) = \underbrace{\frac{1}{1 - \rho_0 c(q)}}_{S(q)}$$

Percus-Yevick's [3] Closure relation in terms of the interatomic potential  $\phi(r)$ 

$$c(r) = g(r) \left[ 1 - e^{\beta \phi(r)} \right] \tag{3}$$

Equations (1) and (2) constitute a set of integral equations

Hard-sphere (HS) potential

$$\phi_{HS}(r) = \begin{cases} \infty & r < d \\ 0 & r > d \end{cases}$$
 (4)

where d is the hard-sphere diameter. In this case the PY integral equation has been solved exactly by M. S. Wertheim [5] and E. Thiele [4] in 1963.

The solution is given in terms of the packing fraction

$$\eta = \frac{\text{volume filled with spheres}}{\text{total volume}} = \frac{\pi}{6} d^3 \rho_0 \tag{5}$$

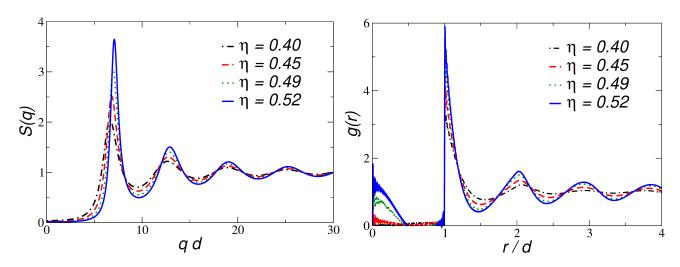
and the dimensionless variable x = r/d

$$c(r) = \begin{cases} \lambda_1 - 6\eta \lambda_2 x + \frac{1}{2}\eta \lambda_1 x^3 & x < 1 \\ 0 & x > 1 \end{cases}, \tag{6}$$

with

$$\lambda_1 = (1 + 2\eta)^2 / (1 - \eta)^4 \tag{7a}$$

$$\lambda_2 = (1 + \frac{1}{2}\eta)^2 / (1 - \eta)^4$$
 (7b)



Hard-sphere Percus-Yevick structure factors S(q) and pair correlation functions g(r) for different packing fractions  $\eta$ 

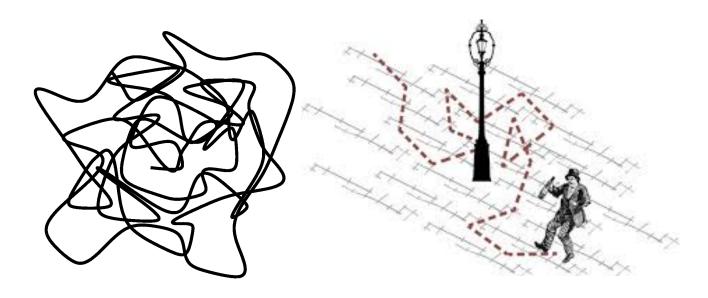
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# 3 Structure of polymers

## Schirmacher 4.3, 6.1

Polymer structure as a random walk:



- 1. Characterize the statistics of a random walk
- 2. Relation with a diffusion process
- 3. Derive thermodynamics of the polymer from the random walk statistics

## 4 Color of glass

## Encyclopedia, 6.2



Figure 1 French stained glass from the thirteenth century (cf. Figure VI). (a) Notre-Dame of Chartres cathedral (1215–1240), Bay 5, James and Josuas, detail of The life of St. James the Greater (cf. Figure VI), Chartres. © Malnoury, Robert; Martin, J., Inventaire général, ADAGP. (b) Sainte Chapelle, Paris (1245–1250). © RMN (Musée de Cluny, Paris). (See electronic version for color figures)

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Georges Calas, Laurence Galoisy and Laurent Cormier

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Encyclopedia, 1.1 - 1.7

Figure 1 The initial melting step in the making of float glass: the 1-m deep bath of raw materials melted by the flames of a cross-fired furnace (Chapter 9.7). Pulls ranging from 500 to 1000 tons/day and mean residence times of at least 24 hours. Electro-fused refractory materials made up of alumina-zirconia-silica in contact with the melt, and of alumina and alumina-silica elsewhere (cf. Chapter 9.8). Source: Photo courtesy Simonpietro Di Pierro, Saint-Gobain Research Paris.

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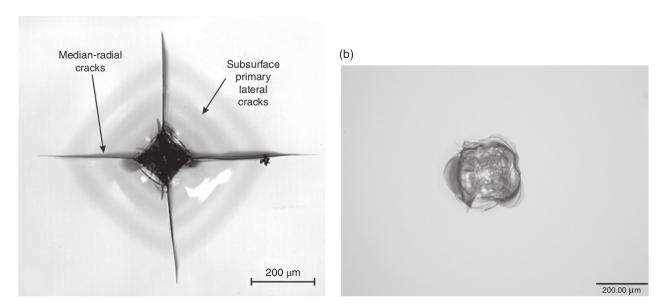
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### 6 Mechanical Properties

### Encyclopedia, 3.11, 3.12



**Figure 5** Contrast between Vicker's indentations on "normal" and "anomalous" glasses. (a) Soda-lime-silica glass showing the centrally deformed region, cross-shaped median-radial cracks as well as primary subsurface lateral cracks, which are visible as interference fringes; (b) fused silica.

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Russell J. Hand

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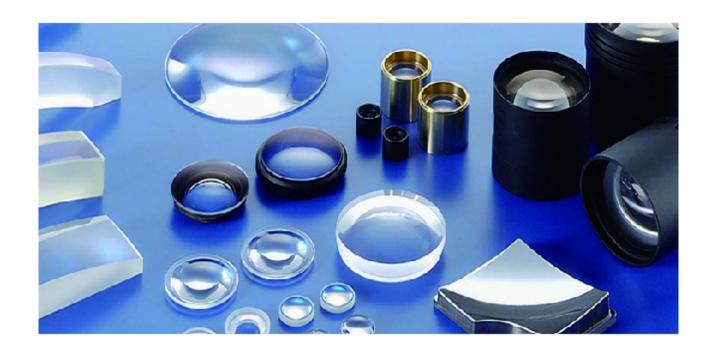
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K. Stefan R. Karlsson and Lothar Wondraczek

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## 7 Optical Properties

## Encyclopedia, 6.1, 6.4



## 6.1 Optical Glasses 665

Alix Clare

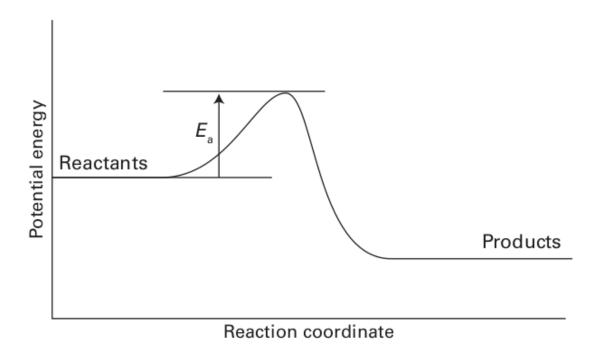
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John Ballato

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## Atkins, Topic 18 C



**Figure 18C.1** A potential energy profile for an exothermic reaction. The height of the barrier between the reactants and products is the activation energy of the reaction.

## 18C.1 The Eyring equation

- (a) The formulation of the equation
- (b) The rate of decay of the activated complex
- (c) The concentration of the activated complex
- (d) The rate constant

## 9 Coherent-Potential Approximation

### Schirmacher, 4.4

Random walk with fluctuating walk rates  $W_{ij}$ :

$$\frac{\mathrm{d}}{\mathrm{d}t}P(\mathbf{r}_n, t) = \sum_{\substack{\ell \\ n, N}} W_{n\ell} \left[ P(\mathbf{r}_\ell, t) - P(\mathbf{r}_n, t) \right]$$

If we set the left side of Eq. (4.43) equal to zero, we obtain the steady-state condition

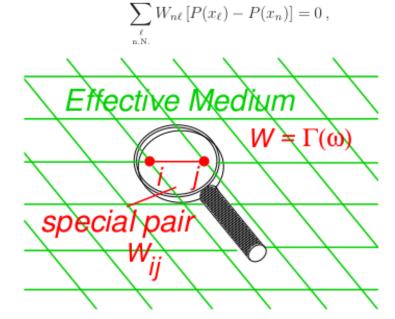
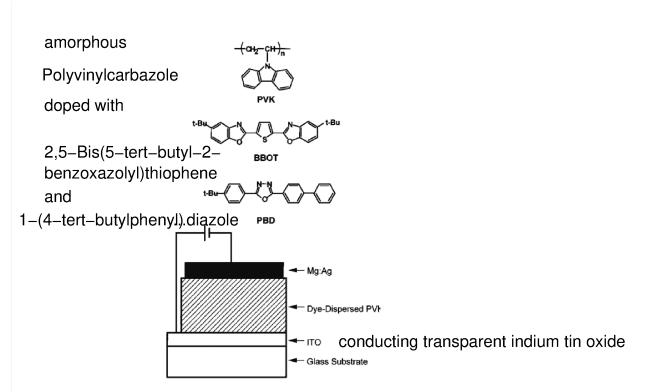


FIG. 4.4: Effective-Medium procedure for the 2-site coherent-potential approximation (CPA)

- 1. Derivation on a cubic lattice
- 2. Modification for a topological disordered system
- 3. calculating the AC conductivity

## 10 Displays and organic light-emitting diodes

### Encyclopedia, 6.10



Device structure and materials used in the first polymer-based white OLED reported by Kido, Shionoya, and Nagai (1995). BBOT and PBD are electron-transporting materials that are added to the hole-transporting PVK matrix to improve carrier balance. From Kido, Shionoya, and Nagai, 1995.

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Kei Maeda

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### 11 Amorphous Ice

## Encyclopedia, 3.14

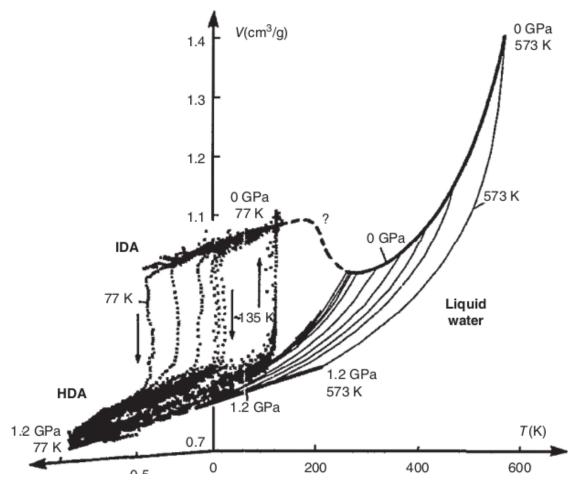


Figure 7 Volume changes as a function of pressure and temperature for the transition between the high- and low-density amorphous ices under nominal pressure of 0.55, 0.45, 0.38, and 0.32 GPa at 77, 100, 121, and 135 K respectively. Liquid water under 1.2 GPa at zero pressure also represented versus temperature.

Connection between LDA and liquid state at zero pressure (e.g. liquid 1) occurring at 227 K. Source: Reproduced with permission from [7], © AIP Publishing.

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Robert F. Tournier

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